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The Crystal Structure of Boron Trifluoride Dihydrate

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The crystal structure of boron trifluoride dihydrate has been determined at 3 °C by X-ray diffraction. The crystals belong to the monoclinic space group $P2_1/c$ and have cell dimensions

 $a = 5.606, b = 7.438, c = 8.683 \text{ Å}; \beta = 90.45^{\circ}.$

 $BF_3.2H_2O$ appears to have a structure with one water molecule bonded to boron to form the molecular addition compound $F_3B.OH_2$; the other water molecule links these together by means of hydrogen bonds. However, the ionic formulation $[H_3O]^+[BF_3OH]^-$ cannot be entirely excluded by the diffraction evidence.

Introduction

The early observation by Klinkenberg & Ketelaar (1935) that the X-ray diffraction pattern of BF₃.2H₂O is very similar to those of NH₄BF₄ and NH₄ClO₄ suggested that the former compound is isomorphous with the latter compounds, and so is probably a hydronium salt in the solid. The presence of H₃O⁺ and BF₃OH⁻ in the liquid was indicated by the conduct-ometric measurements of Greenwood & Martin (1951). It would then be interesting to compare the pattern of hydrogen bonding here with those in other hydronium salts such as H₃OCl (Yoon & Carpenter, 1959) and H₃OClO₄ (Lee & Carpenter, 1959). On the other

hand, Ford & Richards (1956) concluded from nuclear magnetic resonance studies that in slowly crystallized boron trifluoride dihydrate the water molecules are present in molecular complexes. The present structure determination was undertaken to ascertain the true nature of this substance and to investigate the hydrogen bonding pattern. Additional details of this work are presented in a thesis by one of us (Bang, 1963).

Experimental

Boron trifluoride dihydrate, prepared by introducing boron trifluoride gas into water and subsequent fractional crystallization, was sealed in Pyrex glass capillaries. Crystals were grown and preserved in the capillaries by cooling with a stream of cold nitrogen. Crystallization was initiated by touching the capillary lightly with a piece of solid carbon dioxide. By partial melting and refreezing, a satisfactory crystal was obtained; it was used for all diffraction measurements. The b+c direction was along the capillary axis.

A series of precession photographs was prepared with Zr-filtered Mo radiation. The crystal was held at about 3°C, just 3° below the melting point, in order to minimize the formation of frost on the sample and the possibility of the crystal cracking inside the capillary. Both zero and upper layers were recorded for five orientations; for each layer, exposures of 6 hours and of $1\frac{1}{2}$ hours were recorded. Relative intensities were estimated by visual comparison with a standard scale. The 572 observed reflections were placed on a common scale by the method of Rollett & Sparks (1960), the duplicates were averaged, and 191 independent structure factor magnitudes were extracted. This is not quite half of those accessible within the volume of reciprocal space surveyed, but the difficulty of growing and preserving satisfactory crystals of this material would make it very time-consuming to obtain more data.

Unit cell and space group

The crystal was found to be monoclinic, although nearly orthorhombic, and to belong to the space group $P2_1/c$. Unit-cell dimensions were determined from measurements of relatively high-angle diffraction spots on precession photographs of several layers, by means of a least-squares procedure. The resulting dimensions are a=5.606~(0.003), b=7.438~(0.006),c=8.683~(0.005) Å, and $\beta=90.45~(0.12)^{\circ}$; the quantities in parentheses are the estimated standard deviations from the normal equations of the least-squares treatment, and so measure random errors only.

The density calculated from these data for 4 molecules per cell is 1.74 g.cm^{-3} ; this is consistent with the value 1.62 g.cm^{-3} measured pycnometrically for the liquid.

Determination of the structure

Despite the lower symmetry of crystalline boron trifluoride dihydrate relative to hydronium perchlorate (Lee & Carpenter, 1959), these substances were assumed to be approximately isomorphous as implied by the suggested isomorphism with ammonium perchlorate. This gave a trial structure with some atoms at $x=\frac{1}{4}$, the locus of a mirror plane for hydronium perchlorate which is not present in boron trifluoride dihydrate. This structure was refined by a combination of Fourier and least-squares methods to a conventional discrepancy index of 17.2%. At this point the refinement had become very slow, although it had not completely converged, and some of the interatomic distances and temperature parameters seemed unlikely. Consequently it appeared that the previous trial structure was not a satisfactory starting point for refinement, although, from the qualitative similarity of the structure factors to those of hydronium perchlorate, it seemed unlikely that it could be very far from correct. A slightly revised trial structure was therefore formulated, differing chiefly in having the boron atom shifted to the other side of the $x=\frac{1}{4}$ plane from the position to which it had moved in the preceding refinement. A sequence of least-squares refinement cycles, with the introduction of anisotropic temperature parameters for atoms other than boron at an advanced stage, reduced the conventional discrepancy index ultimately to 8.6% for the observed reflections only.

Even with this fully refined structure, it was not possible to distinguish between oxygen and fluorine atoms on the boron atom by structure factor calculations. The same discrepancy was obtained for either choice for atom 4, the one which other structural evidence indicated to be oxygen. The temperature parameters were slightly more consistent with atom 4 identified as oxygen.

It proved to be impossible to locate hydrogen atoms directly and unambiguously by difference synthesis since the background fluctuations were as large as peaks thought to represent hydrogen atoms.

The final atomic coordinates and thermal parameters are listed in Table 1. There the quantities in parentheses are the standard deviations estimated from the diagonal elements of the least-squares normal equations matrix; they are thus somewhat optimistic. The temperature parameters are those in the expression

$$\exp\left[-(\beta_{11}h^2+\beta_{22}k^2+\beta_{33}l^2+\beta_{12}hk+\beta_{23}kl+\beta_{31}lh)\right].$$

The temperature factor was restricted to the isotropic form for the boron atom; consequently the offdiagonal parameters are exactly or very nearly zero.

The observed and calculated structure factors are listed in Table 2. The atomic scattering factors used were that of McWeeny (1951) for boron and those of Berghuis, Haanappel, Potters, Loopstra, MacGillavry & Veenendaal (1955) for oxygen and fluorine.

During the course of the refinement, several different programs and computers were used; the program LSII of Senko & Templeton (1957) for the IBM 650, the program ORXLS of Busing & Levy (1959) for the IBM 704, and the program BXLS of Carpenter (1963) for the IBM 7070 computer.

Description and discussion of the structure

The structure of boron trifluoride dihydrate is illustrated schematically in Fig. 1. The general features are similar to those of hydronium perchlorate (Lee & Carpenter, 1959) except that the latter has mirror planes at $x=\frac{1}{4}$ and $\frac{3}{4}$ passing through the roughly tetrahedral groups of atoms. The details, however, lead to a rather different interpretation.

Table 1. Atomic parameters $(\times 10^4)$ for BF ₃ ·2.	2H,0	BF ₃ ·2	for BF	$\times 10^{4}$) j	parameters	Atomic	Table 1.
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Atom	x	y	z	β_{11}	β_{22}	β_{33}	β_{12}	β_{23}	β_{31}
$\mathbf{F}(1)$	2656(5)	651(4)	3069(4)	300(10)	178(7)	161(6)	-91(16)	-110(9)	122(15)
$\mathbf{F}(2)$	2651(6)	1134(5)	5676(4)	282(12)	282(8)	153(6)	152(18)	173(12)	-2(14)
$\mathbf{F}(3)$	4026(6)	3279(4)	4030(4)	303(12)	208(7)	140(6)	-117(16)	3(11)	-4(14)
O(4)	9910(6)	2703(5)	4140(4)	186(15)	154(8)	156(7)	113(18)	-40(13)	28(16)
O(5)	7472(7)	3168(5)	6642(4)	334(15)	198(9)	104(6)	41(19)	-30(12)	-78(17)
$\mathbf{B}(6)$	2439(12)	1845(9)	4262(8)	237(21)	134(15)	98(12)	0	0	0

Table 2. Observed and calculated structure factors for boron trifluoride dihydrate

hkl Fo Fo hkl Fo Fo 002 173 162 074 71 59 004 298 351 074 71 59 006 128 148 100 -30 -37 008 127 -142 102 490 467 -102 333 -381 -302 -321 -205 011 169 -171 104 297 -205 -205	hkl F _o F _c -143 63 38 144 -60 7 -144 111 -116 145 -60 32 -145 -60 -48 146 -80 -38 -146 77 -81	hkl F _o F _c -215 -60 30 216 83 -109 -216 -60 24 217 -80 -70 220 221 -213 221 358 321	hkl F_0 F_c -255 78 -88 260 -80 -25 -261 100 100 262 -60 -58 -262 -60 -7 -262 -80 70 -263 -80 70	hkl F ₀ F _c -335 80 87 336 -70 19 -336 -70 -16 340 -70 40 341 -70 29 -341 182 -142	hkl F ₀ F _c -414 -70 69 415 -70 32 -415 -60 -23 416 -80 1 -416 -70 52 420 67 -57	hkl F ₀ F _c 504 116 -133 -504 -70 32 510 -70 -33 511 -70 38 -511 -60 72 512 -80 73
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccc} -14.6 & 77 & -81 \\ 14.7 & -80 & -48 \\ 14.8 & -70 & -6 \\ 150 & -70 & -25 \\ 151 & 113 & 74 \\ -151 & 170 & -80 \\ 152 & 157 & 210 \\ -152 & -60 & -29 \\ 153 & 103 & 98 \\ 153 & 103 & 98 \\ 153 & -80 & 34 \end{array}$	221 177 158 222 58 28 -222 123 -116 223 87 -85 -223 51 -50 224 64 65 -224 -70 -47 225 154 -180 -225 -60 -22 226 -70 41 227 -70 18	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{c} -154 \\ 155 \\ 155 \\ 83 \\ -90 \\ -155 \\ 95 \\ 87 \\ 156 \\ 122 \\ -114 \\ \hline 160 \\ -80 \\ -80 \\ -80 \\ -161 \\ -80 \\ 13 \\ 162 \\ -80 \\ 38 \\ -62 \\ -80 \\ -116 \\ \end{array}$	-227 -70 31 230 -50 19 231 -50 -8 -231 227 -235 232 152 -150 -332 111 -121 233 -60 -11 -233 251 -255 234 126 140 -234 148 120	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$
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$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	322 64 -66 -322 62 -69 323 209 205 -323 -60 -23 324 80 78 -324 -70 5 325 85 77 -325 -60 -8 326 -70 63	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	240 87 -64 250 48 -43 251 -70 -28 252 -60 -78 252 -60 -78 253 -80 19 -253 85 77 254 156 125 -254 -70 -78 -255 -70 -78	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$

The values are $10|F|_0$ and $10F_c$ for the model with atom 4 identified as oxygen.

For $|F|_o$ a minus sign indicates an upper limit for an unobserved reflection.

The important interatomic distances and angles are given in Table 3. Standard deviations are about 0.01 Å for distances, about 1.0° for angles. The atoms are labelled to correspond to Fig. 1; these labels are supplemented where necessary by a three-digit code (t_a, t_b, t_c) giving the translations along the a, b, and caxes which specify a particular adjacent unit cell.

Of the four bonds around a boron atom, that to atom 4 is much longer than the others. (This long bond was produced repeatedly by the least-squares refinement despite misguided attempts to force it to become shorter.) This length of 1.565 is comparable to the average value of 1.585 Å reported for B-N distances in three amine-boron trifluoride addition compounds (Hoard, Geller & Owen, 1951), since distances to oxygen should be a little shorter than those to nitrogen. This B–O distance is somewhat longer than the 1.50 ± 0.06 Å in F₃B.O(CH₃)₂ reported by Bauer, Finlay & Laubengayer (1945). No other examples of B–O bonds in similar environments seem to have been reported.

Although the other three bonds to boron differ among themselves by significant amounts, their average 1.370 Å is just the expected value for a B-F bond (Pauling, 1960), is essentially that observed (average 1.39 Å) in the amine-boron trifluorides referred to above, and is much less than the value 1.43 Å found in BF_4^- ion (Pendred & Richards, 1955). It is also less than the value 1.43 Å reported for $F_3B.O(CH_3)_2$ referred to above, but the uncertainties

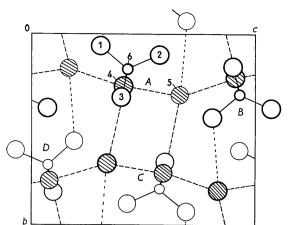


Fig. 1. The structure of boron trifluoride dihydrate viewed along *a*. The small circles are boron atoms, the larger open circles are fluorine atoms, and the shaded circles are oxygen atoms. Heavily outlined atoms lie near $x = \frac{1}{4}$ or $\frac{5}{4}$, lightly outlined ones near $x = \frac{3}{4}$ or $-\frac{1}{4}$.

Table 3. Bond lengths and angles in $BF_3.2 H_2O$

Dimensions in the F₃B.OH₂ molecule

B-F(1)	1·368 Å	B-F(2)	1∙340 Å
B-F(3)	1·402	B-O(4)	1∙565
O(4)-B-F(1)	107·4°	O(4)-B-F(2)	106·7°
O(4)-B-F(3)	104·6	F(3)-B-F(2)	112·0
F(3)-B-F(1)	109·2	F(2)-B-F(1)	115·8

Coordination of the H₂O molecule

${{\rm O-}A(000)4} \atop {{\rm O-}C(000)3} \atop {{\rm O-}A(000)2}$	2·59 Å 2·84 2·97	O-A(000)4 $O-C(0\overline{1}0)1$	2·64 Å 2·85
B B A A A	$\begin{array}{c} (000)4-O-B(000)4\\ (000)4-O-C(000)3\\ (000)4-O-C(0\overline{1}0)1\\ (000)4-O-A(\overline{1}00)3\\ (000)4-O-C(000)3\\ (000)4-O-C(0\overline{1}0)1\\ (000)4-O-A(\overline{1}00)3 \end{array}$	$112 \cdot 1^{\circ} \\ 123 \cdot 2 \\ 72 \cdot 2 \\ 162 \cdot 0 \\ 96 \cdot 1 \\ 87 \cdot 6 \\ 107 \cdot 0 \\ \end{cases}$	

in that electron diffraction study make a discussion of little value.

The pattern of bond lengths found in the present work — B-F shorter than in BF_4^- , B-O rather long suggests the addition compound $F_3B.OH_2$ with atom 4 being oxygen, rather than the ion BF_3OH^- . The other oxygen atom, atom 5, must then represent simply water of hydration. This conclusion agrees with that of Ford & Richards (1956). However, the ionic alternative cannot be entirely excluded on the basis of the diffraction evidence.

These general conclusions receive support by the observed pattern of hydrogen bonds. Most conspicuous are the hydrogen bonds of lengths 2.59 and 2.64 Å linking $F_3B.OH_2$ and H_2O molecules together into infinite chains along the *c* axis; these are shown dashed in Fig. 1. The angles at both oxygen atoms, atoms 4 and 5, are reasonable. The next longer interatomic distances are those of 2.84 and 2.85 Å

from the water molecule (atom 5) to fluorine atoms 3 and 1, respectively; these run approximately along the *b* axis. The bond angles made by the first are reasonable, those by the second rather unlikely.Both cannot represent hydrogen bonds because they are approximately collinear. The bond length B-F(3) is relatively long; it may be lengthened by participating in a hydrogen bond. Accordingly, the first is tentatively considered as a hydrogen bond and shown dashed in Fig. 1.

Although, in the final difference synthesis, the hydrogen atoms are no higher than random background fluctuations, there are such peaks near the interatomic distances considered to be hydrogen bonds, one near oxygen 4 and two near oxygen 5. The other hydrogen atom which should be bonded to oxygen 4 appears not to be engaged in hydrogen bonding; here too a small peak occurs in a plausible location.

All other interatomic distances are appreciably longer than the sums of the appropriate van der Waals radii.

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