

tion. Special thanks are due also to the directors and staffs of the data processing centers who made their facilities available to us. These include Mrs Jeanette Sieg, formerly of the Pittsburgh Board of Education, Mr William B. Kehl of the University of Pittsburgh, Mr William Milburn of the Mellon Bank and Trust Company, and Dr E. B. Weinberger of the Gulf Research Laboratories. We also gratefully acknowledge the generosity of Dr Heinz W. Sternberg who supplied the dicobalt octacarbonyl used in this research.

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The Crystal Structure of Boron Trifluoride Dihydrate

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The crystal structure of boron trifluoride dihydrate has been determined at 3 °C by X-ray diffraction. The crystals belong to the monoclinic space group $P2_1/c$ and have cell dimensions

$$a = 5.606, b = 7.438, c = 8.683 \text{ \AA}; \beta = 90.45^\circ.$$

$\text{BF}_3 \cdot 2\text{H}_2\text{O}$ appears to have a structure with one water molecule bonded to boron to form the molecular addition compound $\text{F}_3\text{B} \cdot \text{OH}_2$; the other water molecule links these together by means of hydrogen bonds. However, the ionic formulation $[\text{H}_3\text{O}]^+[\text{BF}_3\text{OH}]^-$ cannot be entirely excluded by the diffraction evidence.

Introduction

The early observation by Klinkenberg & Ketelaar (1935) that the X-ray diffraction pattern of $\text{BF}_3 \cdot 2\text{H}_2\text{O}$ is very similar to those of NH_4BF_4 and NH_4ClO_4 suggested that the former compound is isomorphous with the latter compounds, and so is probably a hydronium salt in the solid. The presence of H_3O^+ and BF_3OH^- in the liquid was indicated by the conductometric measurements of Greenwood & Martin (1951). It would then be interesting to compare the pattern of hydrogen bonding here with those in other hydronium salts such as H_3OCl (Yoon & Carpenter, 1959) and H_3OClO_4 (Lee & Carpenter, 1959). On the other

hand, Ford & Richards (1956) concluded from nuclear magnetic resonance studies that in slowly crystallized boron trifluoride dihydrate the water molecules are present in molecular complexes. The present structure determination was undertaken to ascertain the true nature of this substance and to investigate the hydrogen bonding pattern. Additional details of this work are presented in a thesis by one of us (Bang, 1963).

Experimental

Boron trifluoride dihydrate, prepared by introducing boron trifluoride gas into water and subsequent fractional crystallization, was sealed in Pyrex glass

capillaries. Crystals were grown and preserved in the capillaries by cooling with a stream of cold nitrogen. Crystallization was initiated by touching the capillary lightly with a piece of solid carbon dioxide. By partial melting and refreezing, a satisfactory crystal was obtained; it was used for all diffraction measurements. The $b+c$ direction was along the capillary axis.

A series of precession photographs was prepared with Zr-filtered Mo radiation. The crystal was held at about 3°C, just 3° below the melting point, in order to minimize the formation of frost on the sample and the possibility of the crystal cracking inside the capillary. Both zero and upper layers were recorded for five orientations; for each layer, exposures of 6 hours and of 1½ hours were recorded. Relative intensities were estimated by visual comparison with a standard scale. The 572 observed reflections were placed on a common scale by the method of Rollett & Sparks (1960), the duplicates were averaged, and 191 independent structure factor magnitudes were extracted. This is not quite half of those accessible within the volume of reciprocal space surveyed, but the difficulty of growing and preserving satisfactory crystals of this material would make it very time-consuming to obtain more data.

Unit cell and space group

The crystal was found to be monoclinic, although nearly orthorhombic, and to belong to the space group $P2_1/c$. Unit-cell dimensions were determined from measurements of relatively high-angle diffraction spots on precession photographs of several layers, by means of a least-squares procedure. The resulting dimensions are $a=5.606$ (0.003), $b=7.438$ (0.006), $c=8.683$ (0.005) Å, and $\beta=90.45$ (0.12)°; the quantities in parentheses are the estimated standard deviations from the normal equations of the least-squares treatment, and so measure random errors only.

The density calculated from these data for 4 molecules per cell is 1.74 g.cm⁻³; this is consistent with the value 1.62 g.cm⁻³ measured pycnometrically for the liquid.

Determination of the structure

Despite the lower symmetry of crystalline boron trifluoride dihydrate relative to hydronium perchlorate (Lee & Carpenter, 1959), these substances were assumed to be approximately isomorphous as implied by the suggested isomorphism with ammonium perchlorate. This gave a trial structure with some atoms at $x=\frac{1}{4}$, the locus of a mirror plane for hydronium perchlorate which is not present in boron trifluoride dihydrate. This structure was refined by a combination of Fourier and least-squares methods to a conventional discrepancy index of 17.2%. At this point the refinement had become very slow, although it had not completely converged, and some of the interatomic distances and temperature parameters seemed unlikely.

Consequently it appeared that the previous trial structure was not a satisfactory starting point for refinement, although, from the qualitative similarity of the structure factors to those of hydronium perchlorate, it seemed unlikely that it could be very far from correct. A slightly revised trial structure was therefore formulated, differing chiefly in having the boron atom shifted to the other side of the $x=\frac{1}{4}$ plane from the position to which it had moved in the preceding refinement. A sequence of least-squares refinement cycles, with the introduction of anisotropic temperature parameters for atoms other than boron at an advanced stage, reduced the conventional discrepancy index ultimately to 8.6% for the observed reflections only.

Even with this fully refined structure, it was not possible to distinguish between oxygen and fluorine atoms on the boron atom by structure factor calculations. The same discrepancy was obtained for either choice for atom 4, the one which other structural evidence indicated to be oxygen. The temperature parameters were slightly more consistent with atom 4 identified as oxygen.

It proved to be impossible to locate hydrogen atoms directly and unambiguously by difference synthesis since the background fluctuations were as large as peaks thought to represent hydrogen atoms.

The final atomic coordinates and thermal parameters are listed in Table 1. There the quantities in parentheses are the standard deviations estimated from the diagonal elements of the least-squares normal equations matrix; they are thus somewhat optimistic. The temperature parameters are those in the expression

$$\exp [- (\beta_{11}h^2 + \beta_{22}k^2 + \beta_{33}l^2 + \beta_{12}hk + \beta_{23}kl + \beta_{31}lh)] .$$

The temperature factor was restricted to the isotropic form for the boron atom; consequently the off-diagonal parameters are exactly or very nearly zero.

The observed and calculated structure factors are listed in Table 2. The atomic scattering factors used were that of McWeeny (1951) for boron and those of Berghuis, Haanappel, Potters, Loopstra, MacGillavry & Veenendaal (1955) for oxygen and fluorine.

During the course of the refinement, several different programs and computers were used; the program LSII of Senko & Templeton (1957) for the IBM 650, the program ORXLS of Busing & Levy (1959) for the IBM 704, and the program BXLS of Carpenter (1963) for the IBM 7070 computer.

Description and discussion of the structure

The structure of boron trifluoride dihydrate is illustrated schematically in Fig. 1. The general features are similar to those of hydronium perchlorate (Lee & Carpenter, 1959) except that the latter has mirror planes at $x=\frac{1}{4}$ and $\frac{3}{4}$ passing through the roughly tetrahedral groups of atoms. The details, however, lead to a rather different interpretation.

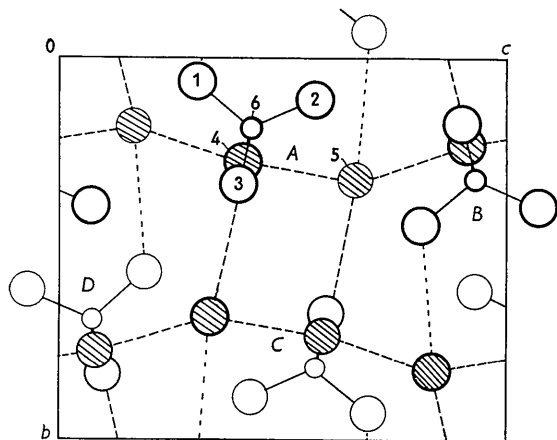


Fig. 1. The structure of boron trifluoride dihydrate viewed along a . The small circles are boron atoms, the larger open circles are fluorine atoms, and the shaded circles are oxygen atoms. Heavily outlined atoms lie near $x = \frac{1}{4}$ or $\frac{3}{4}$, lightly outlined ones near $x = \frac{1}{2}$ or $-\frac{1}{4}$.

Table 3. Bond lengths and angles in $\text{BF}_3 \cdot 2\text{H}_2\text{O}$

Dimensions in the $\text{F}_3\text{B} \cdot \text{OH}_2$ molecule			
B-F(1)	1.368 Å	B-F(2)	1.340 Å
B-F(3)	1.402	B-O(4)	1.565
O(4)-B-F(1)	107.4°	O(4)-B-F(2)	106.7°
O(4)-B-F(3)	104.6	F(3)-B-F(2)	112.0
F(3)-B-F(1)	109.2	F(2)-B-F(1)	115.8

Coordination of the H_2O molecule			
O-A(000)4	2.59 Å	O-A(000)4	2.64 Å
O-C(000)3	2.84	O-C(010)1	2.85
O-A(000)2	2.97		
A(000)4-O-B(000)4	112.1°		
B(000)4-O-C(000)3	123.2		
B(000)4-O-C(010)1	72.2		
B(000)4-O-A(100)3	162.0		
A(000)4-O-C(000)3	96.1		
A(000)4-O-C(010)1	87.6		
A(000)4-O-A(100)3	107.0		

in that electron diffraction study make a discussion of little value.

The pattern of bond lengths found in the present work — B-F shorter than in BF_4^- , B-O rather long — suggests the addition compound $\text{F}_3\text{B} \cdot \text{OH}_2$ with atom 4 being oxygen, rather than the ion BF_3OH^- . The other oxygen atom, atom 5, must then represent simply water of hydration. This conclusion agrees with that of Ford & Richards (1956). However, the ionic alternative cannot be entirely excluded on the basis of the diffraction evidence.

These general conclusions receive support by the observed pattern of hydrogen bonds. Most conspicuous are the hydrogen bonds of lengths 2.59 and 2.64 Å linking $\text{F}_3\text{B} \cdot \text{OH}_2$ and H_2O molecules together into infinite chains along the c axis; these are shown dashed in Fig. 1. The angles at both oxygen atoms, atoms 4 and 5, are reasonable. The next longer interatomic distances are those of 2.84 and 2.85 Å

from the water molecule (atom 5) to fluorine atoms 3 and 1, respectively; these run approximately along the b axis. The bond angles made by the first are reasonable, those by the second rather unlikely. Both cannot represent hydrogen bonds because they are approximately collinear. The bond length B-F(3) is relatively long; it may be lengthened by participating in a hydrogen bond. Accordingly, the first is tentatively considered as a hydrogen bond and shown dashed in Fig. 1.

Although, in the final difference synthesis, the hydrogen atoms are no higher than random background fluctuations, there are such peaks near the interatomic distances considered to be hydrogen bonds, one near oxygen 4 and two near oxygen 5. The other hydrogen atom which should be bonded to oxygen 4 appears not to be engaged in hydrogen bonding; here too a small peak occurs in a plausible location.

All other interatomic distances are appreciably longer than the sums of the appropriate van der Waals radii.

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